

## 3-Hydroxypyridinium hydrogen chloranilate monohydrate

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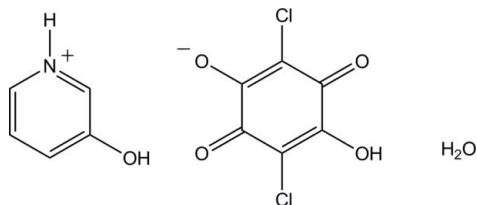
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 Key indicators: single-crystal X-ray study;  $T = 180$  K; mean  $\sigma(\text{C}-\text{C}) = 0.002$  Å;  $R$  factor = 0.030;  $wR$  factor = 0.088; data-to-parameter ratio = 17.8.

In the title salt hydrate,  $\text{C}_5\text{H}_6\text{NO}^+\cdot\text{C}_6\text{HCl}_2\text{O}_4^-\cdot\text{H}_2\text{O}$ , the three components are held together by  $\text{O}-\text{H}\cdots\text{O}$  and  $\text{N}-\text{H}\cdots\text{O}$  hydrogen bonds, as well as by  $\text{C}-\text{H}\cdots\text{O}$  contacts, forming a double-tape structure along the  $c$  axis. Within each tape, the pyridinium ring and the chloranilate ring are almost coplanar, forming a dihedral angle of  $2.35$  ( $7$ )°.

### Related literature

For related structures, see, for example: Gotoh *et al.* (2009*a,b*); Gotoh & Ishida (2009).



### Experimental

#### Crystal data

 $\text{C}_5\text{H}_6\text{NO}^+\cdot\text{C}_6\text{HCl}_2\text{O}_4^-\cdot\text{H}_2\text{O}$ 
 $M_r = 322.10$ 

 Triclinic,  $P\bar{1}$ 
 $a = 7.4893$  (13) Å

 $b = 9.6650$  (17) Å

 $c = 9.9305$  (17) Å

 $\alpha = 88.129$  (5)°

 $\beta = 68.404$  (6)°

 $\gamma = 67.980$  (4)°

 $V = 614.95$  (18) Å<sup>3</sup>
 $Z = 2$ 

 Mo  $K\alpha$  radiation

 $\mu = 0.55$  mm<sup>-1</sup>
 $T = 180$  K

 $0.20 \times 0.15 \times 0.05$  mm

#### Data collection

Rigaku R-Axis RAPID-II diffractometer

 Absorption correction: numerical (*ABSCOR*; Higashi, 1999)

 $T_{\min} = 0.907$ ,  $T_{\max} = 0.973$ 

12237 measured reflections

3572 independent reflections

 2952 reflections with  $I > 2\sigma(I)$ 
 $R_{\text{int}} = 0.025$ 

#### Refinement

 $R[F^2 > 2\sigma(F^2)] = 0.030$ 
 $wR(F^2) = 0.088$ 
 $S = 1.07$ 

3572 reflections

201 parameters

H atoms treated by a mixture of independent and constrained refinement

 $\Delta\rho_{\text{max}} = 0.60$  e Å<sup>-3</sup>
 $\Delta\rho_{\text{min}} = -0.29$  e Å<sup>-3</sup>
**Table 1**

Hydrogen-bond geometry (Å, °).

$D-H\cdots A$	$D-H$	$H\cdots A$	$D\cdots A$	$D-H\cdots A$
$\text{N1}-\text{H1}\cdots\text{O2}^{\text{i}}$	0.911 (18)	1.867 (18)	2.7461 (17)	161.4 (18)
$\text{O4}-\text{H4}\cdots\text{O1}$	0.77 (3)	2.21 (3)	2.6348 (16)	115 (2)
$\text{O4}-\text{H4}\cdots\text{O6}$	0.77 (3)	2.04 (3)	2.7187 (17)	147 (3)
$\text{O5}-\text{H5}\cdots\text{O1}$	0.85 (3)	1.80 (3)	2.6474 (17)	172 (3)
$\text{O6}-\text{H6A}\cdots\text{O2}^{\text{i}}$	0.80 (3)	2.21 (3)	2.8959 (18)	144 (3)
$\text{O6}-\text{H6A}\cdots\text{O3}^{\text{i}}$	0.80 (3)	2.50 (3)	3.1220 (17)	136 (3)
$\text{O6}-\text{H6B}\cdots\text{O1}^{\text{ii}}$	0.84 (4)	2.11 (3)	2.9281 (18)	164 (3)
$\text{C7}-\text{H7}\cdots\text{O6}$	0.95	2.59	3.484 (2)	157
$\text{C9}-\text{H9}\cdots\text{O4}^{\text{iii}}$	0.95	2.40	3.3084 (18)	160
$\text{C10}-\text{H10}\cdots\text{O3}^{\text{iv}}$	0.95	2.38	3.163 (2)	140

Symmetry codes: (i)  $x, y, z - 1$ ; (ii)  $-x + 2, -y + 1, -z$ ; (iii)  $x, y - 1, z$ ; (iv)  $x, y - 1, z - 1$ .

Data collection: *PROCESS-AUTO* (Rigaku/MSC, 2004); cell refinement: *PROCESS-AUTO*; data reduction: *CrystalStructure* (Rigaku/MSC, 2004); program(s) used to solve structure: *SIR92* (Altomare *et al.*, 1994); program(s) used to refine structure: *SHELXL97* (Sheldrick, 2008); molecular graphics: *ORTEP-3* (Farrugia, 1997); software used to prepare material for publication: *CrystalStructure* and *PLATON* (Spek, 2009).

Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: TK2567).

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**supplementary materials**

*Acta Cryst.* (2009). E65, o3060 [ doi:10.1107/S1600536809046844 ]

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#### Comment

The title salt hydrate,  $C_5H_6NO^+ \cdot C_6HCl_2O_4^- \cdot H_2O$ , (I), was prepared in order to extend our study on  $D-H \cdots A$  hydrogen bonding ( $D = N, O$ , or  $C$ ;  $A = N, O$  or  $Cl$ ) in substituted-pyridine – chloranilic acid (systematic name: 2,5-dichloro-3,6-dihydroxy-1,4-benzoquinone) systems (Gotoh & Ishida, 2009; Gotoh *et al.*, 2009*a,b*).

In (I), the three components are held together by  $O-H \cdots O$  and  $N-H \cdots O$  hydrogen bonds, as well as  $C-H \cdots O$  contacts (Fig. 1 and Table 1) forming a double-tape structure along the  $c$  direction. The connections between individual tapes, Fig. 2, are accomplished via  $O_{\text{water}}-H \cdots O$  hydrogen bonds, Fig. 3. Within each tape, the pyridinium  $N1/C7-C11$  and the anion  $C1-C6$  rings are almost coplanar, with a dihedral angle of  $2.35 (7)^\circ$  between them. A  $\pi-\pi$  interaction between the anion rings is also present within the double-tape structure; the centroid-centroid distance [ $Cg1 \cdots Cg1^{iii}$ ; symmetry code: (iii)  $-x + 2, -y + 1, -z + 1$ ] is  $3.6729 (11) \text{ \AA}$  and the inter-planar separation is  $3.2656 (6) \text{ \AA}$ . The double-tapes are connected by  $C-H \cdots O$  contacts, resulting in a layer parallel to the (100) plane, Table 1.

#### Experimental

Single crystals were obtained by slow evaporation from a methanol solution (150 ml) of chloranilic acid (350 mg) and 3-hydroxypyridine (160 mg) at room temperature.

#### Refinement

All H atoms were found in a difference Fourier map and O- and N-bound H atoms were refined isotropically. The refined  $O-H$  and  $N-H$  bond lengths are given in Table 1. C-bound H atoms were positioned geometrically ( $C-H = 0.95 \text{ \AA}$ ) and refined as riding, with  $U_{\text{iso}}(H) = 1.2U_{\text{eq}}(C)$ .

#### Figures

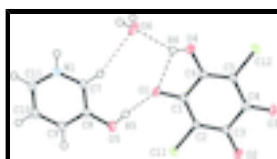


Fig. 1. The molecular structures of the constituents in (I), with the atom-labeling. Displacement ellipsoids of non-H atoms are drawn at the 50% probability level. The dashed lines indicate  $O-H \cdots O$  hydrogen bonds and  $C-H \cdots O$  contacts.

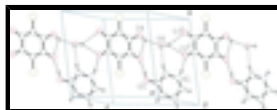


Fig. 2. A partial packing diagram for (I), showing a molecular tape running along the  $c$  axis. The dashed lines indicate  $O-H \cdots O$  and  $N-H \cdots O$  hydrogen bonds, and  $C-H \cdots O$  contacts.



Fig. 3. A partial packing diagram for (I), showing a double-tape structure running along the  $c$  axis. The dashed lines indicate  $O-H \cdots O$  and  $N-H \cdots O$  hydrogen bonds, and  $C-H \cdots O$  contacts. H atoms not involved in the hydrogen bonds have been omitted.

## 3-Hydroxypyridinium hydrogen chloranilate monohydrate

### Crystal data

$C_5H_6NO^+ \cdot C_6HCl_2O_4^- \cdot H_2O$	$Z = 2$
$M_r = 322.10$	$F_{000} = 328.00$
Triclinic, $P\bar{1}$	$D_x = 1.739 \text{ Mg m}^{-3}$
Hall symbol: -P 1	Mo $K\alpha$ radiation, $\lambda = 0.71075 \text{ \AA}$
$a = 7.4893 (13) \text{ \AA}$	Cell parameters from 10001 reflections
$b = 9.6650 (17) \text{ \AA}$	$\theta = 3.0\text{--}30.1^\circ$
$c = 9.9305 (17) \text{ \AA}$	$\mu = 0.55 \text{ mm}^{-1}$
$\alpha = 88.129 (5)^\circ$	$T = 180 \text{ K}$
$\beta = 68.404 (6)^\circ$	Block, brown
$\gamma = 67.980 (4)^\circ$	$0.20 \times 0.15 \times 0.05 \text{ mm}$
$V = 614.95 (18) \text{ \AA}^3$	

### Data collection

Rigaku R-Axis RAPID-II diffractometer	3572 independent reflections
Detector resolution: $10.00 \text{ pixels mm}^{-1}$	2952 reflections with $I > 2\sigma(I)$
$T = 180 \text{ K}$	$R_{\text{int}} = 0.025$
$\omega$ scans	$\theta_{\text{max}} = 30.0^\circ$
Absorption correction: numerical (ABSCOR; Higashi, 1999)	$h = -10 \rightarrow 10$
$T_{\text{min}} = 0.907$ , $T_{\text{max}} = 0.973$	$k = -13 \rightarrow 13$
12237 measured reflections	$l = -13 \rightarrow 13$

### Refinement

Refinement on $F^2$	Secondary atom site location: difference Fourier map
Least-squares matrix: full	Hydrogen site location: inferred from neighbouring sites
$R[F^2 > 2\sigma(F^2)] = 0.030$	H atoms treated by a mixture of independent and constrained refinement
$wR(F^2) = 0.088$	$w = 1/[\sigma^2(F_o^2) + (0.0481P)^2 + 0.2238P]$
$S = 1.07$	where $P = (F_o^2 + 2F_c^2)/3$
3572 reflections	$(\Delta/\sigma)_{\text{max}} < 0.001$
201 parameters	$\Delta\rho_{\text{max}} = 0.60 \text{ e \AA}^{-3}$
Primary atom site location: structure-invariant direct methods	$\Delta\rho_{\text{min}} = -0.29 \text{ e \AA}^{-3}$
	Extinction correction: none

*Special details*

**Geometry.** All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

**Refinement.** Refinement of  $F^2$  against ALL reflections. The weighted  $R$ -factor  $wR$  and goodness of fit  $S$  are based on  $F^2$ , conventional  $R$ -factors  $R$  are based on  $F$ , with  $F$  set to zero for negative  $F^2$ . The threshold expression of  $F^2 > \sigma(F^2)$  is used only for calculating  $R$ -factors(gt) *etc.* and is not relevant to the choice of reflections for refinement.  $R$ -factors based on  $F^2$  are statistically about twice as large as those based on  $F$ , and  $R$ -factors based on ALL data will be even larger.

*Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters ( $\text{\AA}^2$ )*

	<i>x</i>	<i>y</i>	<i>z</i>	$U_{\text{iso}}^*/U_{\text{eq}}$
C11	0.74975 (5)	0.30013 (3)	0.52240 (3)	0.01897 (9)
C12	0.76493 (5)	0.94942 (3)	0.44706 (4)	0.02295 (10)
O1	0.77201 (16)	0.47186 (11)	0.26178 (10)	0.0198 (2)
O2	0.72724 (17)	0.51208 (11)	0.74674 (10)	0.0226 (2)
O3	0.73261 (17)	0.78687 (12)	0.71214 (11)	0.0244 (2)
O4	0.76878 (18)	0.74463 (12)	0.23264 (11)	0.0238 (2)
O5	0.7211 (2)	0.21895 (12)	0.23481 (11)	0.0277 (2)
O6	0.8140 (2)	0.62351 (14)	-0.02703 (12)	0.0284 (2)
N1	0.7338 (2)	0.25226 (14)	-0.13073 (13)	0.0229 (2)
C1	0.76153 (19)	0.53710 (14)	0.37347 (13)	0.0153 (2)
C2	0.7509 (2)	0.47845 (13)	0.50577 (13)	0.0152 (2)
C3	0.7388 (2)	0.55870 (14)	0.62593 (13)	0.0162 (2)
C4	0.7419 (2)	0.71690 (14)	0.60863 (14)	0.0173 (2)
C5	0.7570 (2)	0.77458 (14)	0.46900 (14)	0.0168 (2)
C6	0.7618 (2)	0.69224 (14)	0.35935 (14)	0.0165 (2)
C7	0.7293 (2)	0.29123 (15)	-0.00035 (15)	0.0199 (3)
H7	0.7272	0.3870	0.0215	0.024*
C8	0.7279 (2)	0.18979 (15)	0.10182 (14)	0.0190 (3)
C9	0.7317 (2)	0.05028 (15)	0.06603 (15)	0.0222 (3)
H9	0.7297	-0.0203	0.1348	0.027*
C10	0.7383 (2)	0.01496 (16)	-0.06979 (16)	0.0239 (3)
H10	0.7428	-0.0805	-0.0954	0.029*
C11	0.7382 (2)	0.11952 (17)	-0.16830 (15)	0.0252 (3)
H11	0.7413	0.0970	-0.2617	0.030*
H1	0.731 (3)	0.328 (2)	-0.188 (2)	0.041 (6)*
H6A	0.759 (4)	0.633 (3)	-0.084 (3)	0.067 (8)*
H6B	0.941 (5)	0.594 (3)	-0.081 (3)	0.061 (8)*
H4	0.762 (4)	0.690 (3)	0.182 (3)	0.063 (8)*
H5	0.739 (4)	0.301 (3)	0.235 (3)	0.060 (7)*

## supplementary materials

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### Atomic displacement parameters ( $\text{\AA}^2$ )

	$U^{11}$	$U^{22}$	$U^{33}$	$U^{12}$	$U^{13}$	$U^{23}$
C11	0.02939 (17)	0.01539 (14)	0.01838 (15)	-0.01195 (12)	-0.01284 (12)	0.00521 (11)
C12	0.03172 (18)	0.01444 (15)	0.02679 (18)	-0.01173 (13)	-0.01295 (14)	0.00362 (11)
O1	0.0324 (5)	0.0193 (4)	0.0138 (4)	-0.0142 (4)	-0.0113 (4)	0.0028 (3)
O2	0.0366 (6)	0.0214 (5)	0.0159 (4)	-0.0141 (4)	-0.0140 (4)	0.0051 (4)
O3	0.0360 (6)	0.0239 (5)	0.0181 (5)	-0.0149 (4)	-0.0120 (4)	-0.0016 (4)
O4	0.0443 (6)	0.0186 (5)	0.0171 (5)	-0.0168 (4)	-0.0166 (4)	0.0069 (4)
O5	0.0531 (7)	0.0237 (5)	0.0208 (5)	-0.0232 (5)	-0.0218 (5)	0.0071 (4)
O6	0.0357 (6)	0.0369 (6)	0.0159 (5)	-0.0149 (5)	-0.0124 (5)	0.0023 (4)
N1	0.0314 (6)	0.0236 (6)	0.0174 (5)	-0.0136 (5)	-0.0106 (5)	0.0073 (4)
C1	0.0189 (6)	0.0146 (5)	0.0145 (5)	-0.0077 (4)	-0.0076 (4)	0.0027 (4)
C2	0.0212 (6)	0.0130 (5)	0.0145 (6)	-0.0081 (4)	-0.0088 (5)	0.0029 (4)
C3	0.0192 (6)	0.0162 (5)	0.0152 (6)	-0.0077 (5)	-0.0079 (5)	0.0023 (4)
C4	0.0204 (6)	0.0180 (6)	0.0157 (6)	-0.0086 (5)	-0.0080 (5)	0.0011 (4)
C5	0.0218 (6)	0.0128 (5)	0.0185 (6)	-0.0086 (5)	-0.0088 (5)	0.0030 (4)
C6	0.0221 (6)	0.0152 (5)	0.0150 (6)	-0.0091 (5)	-0.0086 (5)	0.0043 (4)
C7	0.0272 (7)	0.0171 (6)	0.0191 (6)	-0.0114 (5)	-0.0101 (5)	0.0034 (5)
C8	0.0261 (7)	0.0181 (6)	0.0170 (6)	-0.0111 (5)	-0.0103 (5)	0.0026 (5)
C9	0.0340 (7)	0.0181 (6)	0.0202 (6)	-0.0134 (5)	-0.0134 (6)	0.0049 (5)
C10	0.0335 (7)	0.0206 (6)	0.0219 (7)	-0.0137 (6)	-0.0118 (6)	0.0002 (5)
C11	0.0344 (8)	0.0295 (7)	0.0162 (6)	-0.0157 (6)	-0.0113 (5)	0.0023 (5)

### Geometric parameters ( $\text{\AA}$ , $^\circ$ )

C11—C2	1.7289 (13)	C1—C2	1.4007 (17)
C12—C5	1.7172 (13)	C1—C6	1.5020 (17)
O1—C1	1.2564 (15)	C2—C3	1.4006 (17)
O2—C3	1.2519 (15)	C3—C4	1.5412 (18)
O3—C4	1.2149 (16)	C4—C5	1.4587 (18)
O4—C6	1.3313 (15)	C5—C6	1.3514 (18)
O4—H4	0.76 (3)	C7—C8	1.3877 (18)
O5—C8	1.3381 (16)	C7—H7	0.9500
O5—H5	0.85 (3)	C8—C9	1.3930 (18)
O6—H6A	0.80 (3)	C9—C10	1.3808 (19)
O6—H6B	0.84 (3)	C9—H9	0.9500
N1—C11	1.3330 (19)	C10—C11	1.383 (2)
N1—C7	1.3452 (18)	C10—H10	0.9500
N1—H1	0.91 (2)	C11—H11	0.9500
C6—O4—H4	111 (2)	C4—C5—C12	119.01 (9)
C8—O5—H5	106.0 (18)	O4—C6—C5	121.39 (11)
H6A—O6—H6B	103 (3)	O4—C6—C1	116.69 (11)
C11—N1—C7	123.32 (12)	C5—C6—C1	121.91 (11)
C11—N1—H1	125.1 (14)	N1—C7—C8	119.14 (12)
C7—N1—H1	111.6 (14)	N1—C7—H7	120.4
O1—C1—C2	126.22 (11)	C8—C7—H7	120.4

O1—C1—C6	115.16 (11)	O5—C8—C7	123.49 (12)
C2—C1—C6	118.62 (11)	O5—C8—C9	117.59 (12)
C3—C2—C1	122.83 (11)	C7—C8—C9	118.92 (12)
C3—C2—C11	118.48 (9)	C10—C9—C8	119.78 (13)
C1—C2—C11	118.68 (9)	C10—C9—H9	120.1
O2—C3—C2	125.37 (12)	C8—C9—H9	120.1
O2—C3—C4	116.88 (11)	C9—C10—C11	119.55 (13)
C2—C3—C4	117.75 (11)	C9—C10—H10	120.2
O3—C4—C5	123.42 (12)	C11—C10—H10	120.2
O3—C4—C3	118.12 (11)	N1—C11—C10	119.29 (13)
C5—C4—C3	118.46 (10)	N1—C11—H11	120.4
C6—C5—C4	120.38 (11)	C10—C11—H11	120.4
C6—C5—C12	120.61 (10)		
O1—C1—C2—C3	-179.78 (13)	C4—C5—C6—O4	177.85 (12)
C6—C1—C2—C3	0.53 (19)	C12—C5—C6—O4	-1.29 (19)
O1—C1—C2—C11	-0.50 (19)	C4—C5—C6—C1	-2.7 (2)
C6—C1—C2—C11	179.80 (9)	C12—C5—C6—C1	178.13 (10)
C1—C2—C3—O2	179.38 (13)	O1—C1—C6—O4	1.29 (17)
C11—C2—C3—O2	0.10 (19)	C2—C1—C6—O4	-178.98 (12)
C1—C2—C3—C4	-1.25 (19)	O1—C1—C6—C5	-178.16 (12)
C11—C2—C3—C4	179.47 (9)	C2—C1—C6—C5	1.57 (19)
O2—C3—C4—O3	-0.19 (19)	C11—N1—C7—C8	-0.4 (2)
C2—C3—C4—O3	-179.62 (12)	N1—C7—C8—O5	-179.23 (13)
O2—C3—C4—C5	179.52 (12)	N1—C7—C8—C9	0.2 (2)
C2—C3—C4—C5	0.09 (18)	O5—C8—C9—C10	179.88 (14)
O3—C4—C5—C6	-178.41 (13)	C7—C8—C9—C10	0.5 (2)
C3—C4—C5—C6	1.89 (19)	C8—C9—C10—C11	-0.9 (2)
O3—C4—C5—C12	0.74 (19)	C7—N1—C11—C10	0.0 (2)
C3—C4—C5—C12	-178.96 (9)	C9—C10—C11—N1	0.6 (2)

Hydrogen-bond geometry ( $\text{\AA}$ ,  $^\circ$ )

<i>D</i> —H... <i>A</i>	<i>D</i> —H	H... <i>A</i>	<i>D</i> ... <i>A</i>	<i>D</i> —H... <i>A</i>
N1—H1...O2 <sup>i</sup>	0.911 (18)	1.867 (18)	2.7461 (17)	161.4 (18)
O4—H4...O1	0.77 (3)	2.21 (3)	2.6348 (16)	115 (2)
O4—H4...O6	0.77 (3)	2.04 (3)	2.7187 (17)	147 (3)
O5—H5...O1	0.85 (3)	1.80 (3)	2.6474 (17)	172 (3)
O6—H6A...O2 <sup>i</sup>	0.80 (3)	2.21 (3)	2.8959 (18)	144 (3)
O6—H6A...O3 <sup>i</sup>	0.80 (3)	2.50 (3)	3.1220 (17)	136 (3)
O6—H6B...O1 <sup>ii</sup>	0.84 (4)	2.11 (3)	2.9281 (18)	164 (3)
C7—H7...O6	0.95	2.59	3.484 (2)	157
C9—H9...O4 <sup>iii</sup>	0.95	2.40	3.3084 (18)	160
C10—H10...O3 <sup>iv</sup>	0.95	2.38	3.163 (2)	140

Symmetry codes: (i)  $x, y, z-1$ ; (ii)  $-x+2, -y+1, -z$ ; (iii)  $x, y-1, z$ ; (iv)  $x, y-1, z-1$ .

Fig. 1

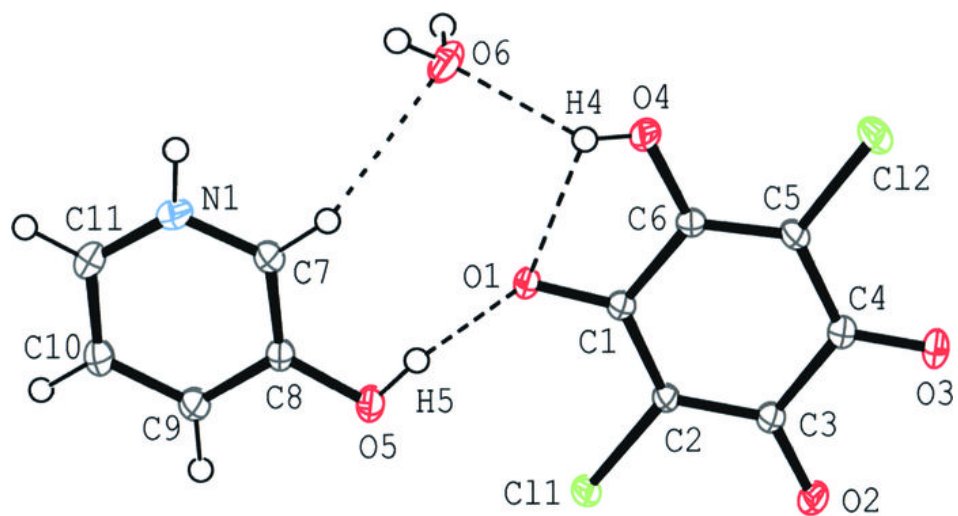




Fig. 2

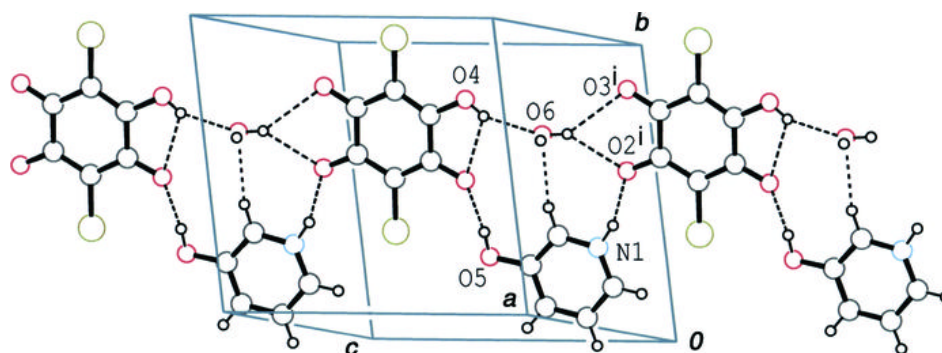


Fig. 3

